

Anti-coincidence Shielding γ -ray Detector based on $\text{LaBr}_3(\text{Ce})/\text{CsI}(\text{TI})$ Phoswich Scintillator*

JiFei Lu,¹ Yun Zheng,^{2,†} LiHua Zhu,^{1,‡} HaoTian Qi,¹ Xuan Pang,¹ Lin Song,¹ DeXing Kong,¹ BaoHua Sun,¹ TianXiao Li,² CongBo Li,² XiaoGuang Wu,² and JingBin Lu³

¹*School of Physics, Beihang University, Beijing 100191, China*

²*China Institute of Atomic Energy, Beijing 102413, China*

³*College of Physics, Jilin University, Jilin 130012, China*

An anti-coincidence shielding γ -ray detector has been designed to study Compton suppression and cosmic rays anti-coincidence based on a $\text{LaBr}_3(\text{Ce})/\text{CsI}(\text{TI})$ phoswich scintillator, where the $\text{LaBr}_3(\text{Ce})$ scintillator is chosen as the main crystal completely surrounded by the $\text{CsI}(\text{TI})$ scintillator. Since the differences in their pulse shapes, a series of studies have been conducted using pulse shape analysis (PSA) methods. By using digital charge integration (QDC), the energy resolutions of the detector are obtained, being 3.7% for 662 keV of ^{137}Cs , 3.1% for 1173 keV and 2.8% for 1332 keV of ^{60}Co after excluding the influence of cascade γ rays. This detector can suppress the Compton continuum by 2~5 times for $^{137}\text{Cs}/^{60}\text{Co}$ based on Fast and Slow Component Ratios (FCR-SCR). Furthermore, almost all cosmic rays can be rejected by filtering events above 10 MeV in an in-beam spectrum analysis. It clearly shows that this anti-coincidence shielding γ -ray detector can be used for low level radioactivity measurements as well as high energy γ rays measurements.

Keywords: phoswich detector, Compton suppression, anti-coincidence shielding, PSA, FCR-SCR

I. INTRODUCTION

In nuclear physics experiments, anti-coincidence shielding usually has two important functions: on one hand, it refers to Compton suppression, and on the other hand, it serves as shielding against cosmic rays in high-energy γ rays measurements. The Compton continuums are the main source of noise in the energy spectra which can reduce the peak-to-total (P/T) ratio of observed low-energy photopeaks and even swamp the smaller ones. Especially in the study of nuclear spectroscopy, this will reduce the sensitivity of the detection of low-energy regions and affect the accuracy of energy spectrum analysis [1]. Therefore, the suppression of the Compton continuum becomes an important factor in improving the sensitivity of low-energy regions. For example, the Compton-suppressed spectrometers made up of a high energy resolution Ge detector assisted by scintillation detectors can be used to measure γ spectra with energies lower than 2 MeV [2~5]. These scintillation detectors are arranged around the Ge detector to capture scattering events, and then veto such events during data processing, thereby achieving a cleaner energy spectrum to facilitate the analysis and research.

Moreover, effective suppression of cosmic ray backgrounds constitutes an essential requirement in a specific high-energy γ -ray detection system. γ rays with energy higher than 10 MeV are significantly influenced by cosmic rays, as the measurement efficiency for these events is very low. For example, the study of the Giant Dipole Resonance (GDR) using fusion evaporation reactions is of great significance for understanding the ground state deformation of atomic nuclei [6~10]. However, in the measurement of GDR γ spectra, the corresponding high-energy γ yield is very low,

approximately $10^{-3} \sim 10^{-4}$ of the neutron yield. As a result, experimental observations are severely affected by cosmic rays, making it difficult to measure accurately and even completely swamped by the cosmic ray components. In the conventional experimental setup, organic scintillator detectors are usually arranged around the main detector(such as $\text{NaI}(\text{TI})$, BGO , BaF_2 and so on) to veto the cosmic ray events, thereby achieving optimal energy spectra. However, both of these traditional measurement systems have complex equipment conditions and the placement of the shielding detectors is also constrained by spatial limitations. This undoubtedly has a certain degree of inconvenience for the experiment. Today, the hardware requirements of data acquisition have been simplified greatly due to the rapid development of digital acquisition systems [11, 12]. Some inorganic scintillators with even better resolution also emerged during the same period [13]. These conditions have facilitated the development of detectors toward greater functionality and portability.

To simplify complex equipment conditions while still achieving the anti-coincidence effect, some researchers have developed novel phoswich detectors by combining all kinds of inorganic scintillators and analyzing experimental data using the pulse shape analysis (PSA) method [14], such as $\text{LaBr}_3(\text{Ce}) + \text{NaI}$ [15], $\text{GAGG} + \text{CsI}(\text{TI})$ [16], $\text{CsI}(\text{TI}) + \text{BGO}$ [17]. These types of detectors, which are aimed at Compton suppression, usually use two inorganic scintillators for the scintillation material. This is mainly because inorganic scintillators can be manufactured in various shapes and have a higher density, making them more effective at capturing Compton scattering events. Among them, the one with better resolution and relatively fast decay time is selected as the main crystal embedded in the well-typed shielding crystal and shares a PMT with performance matching the main crystal [18]. Therefore, the analysis is primarily based on events from the main crystal. In addition, an entrance window can also be implemented for improving the efficiency of capturing large-angle Compton suppression [16].

This paper presents research work related to the phoswich

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† Corresponding author, zhengyun@ciae.ac.cn

‡ Corresponding author, zhulh@buaa.edu.cn

70 detector to realize both Compton suppression and cosmic rays
 71 anti-coincidence, which utilizes the $\text{LaBr}_3(\text{Ce})/\text{CsI}(\text{TI})$ scin-
 72 tillator combinations. The $\text{LaBr}_3(\text{Ce})$ scintillator is chosen
 73 as the main crystal because of its excellent energy resolution
 74 ($\sim 3\%$ for 662 keV) and fast decay time (~ 16 ns) [19]. The
 75 $\text{CsI}(\text{TI})$ scintillator serving as the shielding crystal has a high
 76 effective Z and density, allowing it to effectively capture scat-
 77 tering events. Moreover, its decay time (~ 1000 ns) is much
 78 longer than that of $\text{LaBr}_3(\text{Ce})$, making pulse shape discrimi-
 79 nation (PSD) easier [20]. The effect of Compton suppression
 80 in the low energy region was carefully studied by using pulse
 81 analysis methods. Furthermore, an in-beam experiment of the
 82 fusion evaporation reaction (52 MeV $^{11}\text{B} + ^{142}\text{Ce}$) was con-
 83 ducted to verify the anti-coincidence of cosmic rays in the
 84 high energy region. The content consists of the following
 85 components:

86 Section II presents the principle of the phoswich detector
 87 and the design of the $\text{LaBr}_3(\text{Ce})/\text{CsI}(\text{TI})$ phoswich scin-
 88 tillator. In Sect. III, we introduce the experiments and results,
 89 including $^{60}\text{Co}/^{137}\text{Cs}$ measurements and the in-beam mea-
 90 surement. In Sect. IV, we discuss the energy resolution of
 91 cascade γ rays, the ability of Compton suppression, and cos-
 92 mic rays anti-coincidence. A summary is provided in Sect.
 93 IV.

94 II. METHOD AND SETUP

95 A. Principle of the phoswich detector

96 For an anti-coincidence shielding phoswich detector, the
 97 main crystal is usually surrounded by a shielding crystal [15].
 98 The schematic diagram of the phoswich detector is shown in
 99 Fig. 1. The shape of the main crystal (blue) is cylindrical
 100 while the shield crystal should be well-typed (yellow). In or-
 101 der to capture scattering events in a 4π space, there is also an
 102 entrance window (dark yellow). Both of these two scin-
 103 tillators share only one PMT that is suitable for the main crystal.
 104 Therefore, the results of the analysis tend to the characteris-
 105 tics of the main crystal.

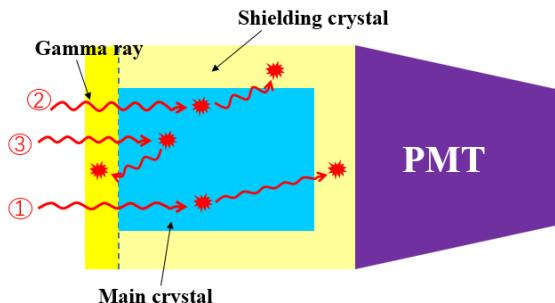


Fig. 1. Schematic diagram of the phoswich detector.

106 The shielding crystal has two important characteristics:
 107 1) The part of it located between the main crystal and the PMT
 108 window can be used to capture small-angle scattering events.
 109 2) The entrance window of it helps to capture back-scattering

110 events. However, the entrance window will have a certain
 111 absorption effect on γ rays, reducing the peak-to-total ratio
 112 of the main crystal and affecting the measurement efficiency
 113 [21].

114 Unlike traditional analog circuitry for acquiring data, this
 115 phoswich detector requires a digital acquisition system to col-
 116 lect pulses and use PSA methods to distinguish events be-
 117 tween three types of crystals [22]. The output pulses can be
 118 accurately described by Eq. 1 without considering the PMT
 119 time fluctuations [23].

$$120 \quad V(t) = \begin{cases} -\frac{GN_eR}{\tau - \tau_s} [e^{-\frac{t}{\tau_s}} - e^{-\frac{t}{\tau}}] & \text{if } \tau \neq \tau_s \\ \left(\frac{GN_eR}{\tau_s^2}\right) \cdot t \cdot e^{-\frac{t}{\tau_s}} & \text{if } \tau = \tau_s \end{cases} \quad (1)$$

121 Where G, e, R represent the gain of the PMT, charge of the
 122 electron and the resistance in the circuit, respectively; N rep-
 123 resents the number of photoelectrons emitted by the cathode,
 124 proportional to the product of energy and light yield; τ_s and
 125 τ represent the decay time of the scintillator and the output
 126 circuit time constant, respectively. Table 1 provides a com-
 127 parison of various typical inorganic scintillators, including
 128 density, maximum emission wavelength and fluorescence de-
 129 cay time [19, 24]. By analyzing the pulses of these common
 130 scintillators through calculations, suitable selections can be
 131 determined.

Table 1. Properties of commonly used typical inorganic scintillation crystals.

Material	Density (g/cm^3)	λ_{max} (nm)	Decay time (ns)	Light yield (Ph/MeV)
NaI(Tl)	3.67	415	230	38000
CsI(Tl)	4.51	550	1000	54000
BGO	7.13	480	300	9000
GAGG	6.63	520	100	56000
LSO	7.4	420	40	27000
$\text{LaBr}_3(\text{Ce})$	5.29	358	16	61000
GSO	6.7	440	60	12500

132 By setting the τ constant to 20 ns and the same energy con-
 133 dition in the calculation, the pulses for different crystals were
 134 formulated using Eq. 1 shown in Fig. 2. The τ is set so short
 135 to ensure that the pulse reflects its decay time characteristics
 136 in the falling edge, which is beneficial for shape discrimina-
 137 tion.

138 From Fig. 2, it is evident that crystals with short decay
 139 times and high light yields generate tall and narrow pulses,
 140 whereas those with long decay times and low light yields pro-
 141 duce short and wide pulses. The differences in pulse charac-
 142 teristics among various crystals are crucial for realizing PSD.

143 B. Pulse Analysis Method

144 Since the phoswich detector has two scintillators, it outputs
 145 pulses of different shapes that need to be discriminated. One
 146 method called Fast and Slow Component Ratios (FCR-SCR)
 147 can be used to separate pulses with different falling edges,

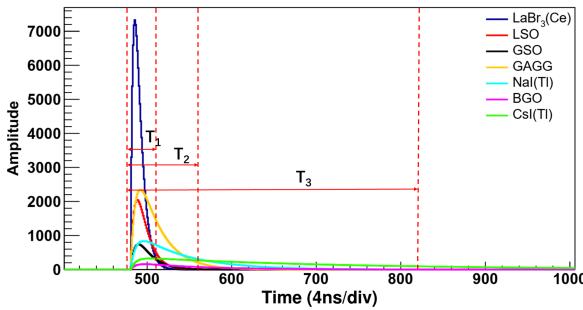


Fig. 2. The pulses for different scintillators formulated by Eq. 1. Different intervals marked as T_1 , T_2 , and T_3 are also shown for integration.

148 which is based on the Charge Comparison Method (CCM).
149 Taking Fig. 2 as an example, the pulses are divided into
150 different integration segments by setting different time nodes
151 within the time window. To calculate values of the fast com-
152 ponent ratio (FCR) and slow component ratio (SCR) of each
153 pulse, first determine the starting point, which is before the
154 pulse trigger point. Then, integrate over intervals T_1 , T_2 , and
155 T_3 to obtain the integral values S_1 , S_2 , and S_3 for each inter-
156 val, respectively. The intervals are set according to the pulse
157 width of the main crystal. Finally, the FCR and SCR can be
158 obtained by the following equation.

$$159 \quad FCR = \frac{S_1}{S_2} \quad (2)$$

$$161 \quad SCR = \frac{S_2}{S_3} \quad (3)$$

162 It is worth noting that Eq. 3 is a modified version of the
163 formula from [14]. The appropriate choice of the integration
164 range can reduce the effect of baseline fluctuations on the in-
165 tegration results in practice. Since there is an inclusion rela-
166 tionship among S_1 , S_2 , and S_3 , the range of both FCR and
167 SCR is $0 \sim 1$.

168 Fig. 3 shows the distribution of different scintillators in
169 the FCR-SCR two-dimension plot. The integral values of T_1 ,
170 T_2 , and T_3 are 120 ns, 240 ns, and 1200 ns, respectively. In
171 this condition, integral segment T_1 can almost fully integrate
172 the $\text{LaBr}_3(\text{Ce})$ pulse, so its values of the FCR or the SCR are
173 near 1. From Fig. 3, the $\text{LaBr}_3(\text{Ce})$ scintillator and $\text{CsI}(\text{TI})$
174 scintillator can be selected as an excellent combination for the
175 phoswich scintillator because of the excellent discrimination
176 between them.

C. The $\text{LaBr}_3(\text{Ce})/\text{CsI}(\text{TI})$ phoswich Scintillator

178 The schematic diagram of the $\text{LaBr}_3(\text{Ce})/\text{CsI}(\text{TI})$ phoswich
179 scintillator is shown in Fig. 4a based on the design concept in
180 Fig. 1. The inner $\text{LaBr}_3(\text{Ce})$ cylindrical crystal has a height

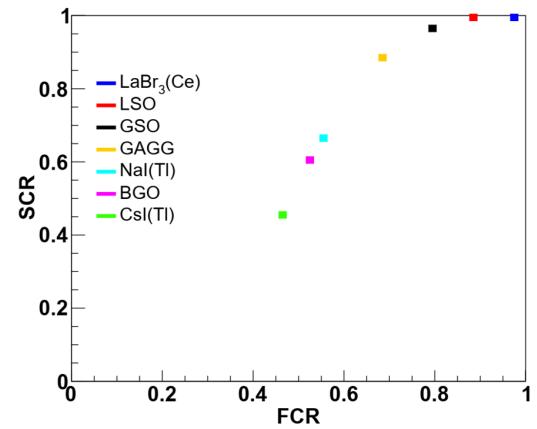


Fig. 3. Distribution of different scintillators in the FCR-SCR two-dimension plot.

181 of 5.0 cm and a radius of 1.9 cm. It is embedded in the well-
182 typed $\text{CsI}(\text{TI})$ crystal, which has a height of 7.0 cm (including
183 a 1.0 cm thick top layer) and a radius of 3.8 cm. The optical
184 silicon grease coupling of the EJ550 model is used between them.
185

186 The image of the phoswich detector is shown in Fig. 4b af-
187 ter encapsulation. The selected photomultiplier tube (PMT)
188 model is Hamamatsu's R6233, with a matching voltage di-
189 vider model E1198-27. The detector is enclosed in a magnetic
190 shielding case of model E989-15 and provides some shade. τ
191 (~ 23 ns) of this PMT base is fast, making it suitable for the
192 $\text{LaBr}_3(\text{Ce})$ scintillator. The outer silver-white aluminum cas-
193 ing also provides some electron absorption.

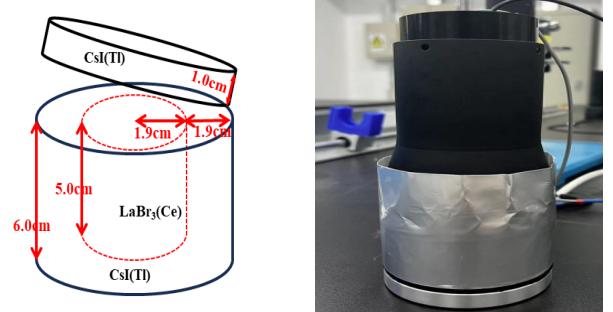


Fig. 4. (a) Schematic diagram of the $\text{LaBr}_3(\text{Ce})/\text{CsI}(\text{TI})$ phoswich scintillator; (b) Image of the phoswich detector.

194 The prediction of the phoswich detector pulses is shown in
195 Fig. 5a. Among them, the $\text{LaBr}_3(\text{Ce})$ pulse is represented in
196 black, the $\text{CsI}(\text{TI})$ pulse in blue, and the $\text{LaBr}_3(\text{Ce})+\text{CsI}(\text{TI})$
197 pulse in red. The latter is also referred to as the "coincidence
198 pulse". The τ set during the calculation process is 20 ns to
199 match $\text{LaBr}_3(\text{Ce})$ decay time. Therefore, the $\text{CsI}(\text{TI})$ pulse
200 will be significantly less than the $\text{LaBr}_3(\text{Ce})$ pulse in terms of
201 amplitude. It is also seen that the tail of the coincidence pulse
202 is from the contribution of $\text{CsI}(\text{TI})$ and the front part mainly
203 from $\text{LaBr}_3(\text{Ce})$. In the calculation, the energy of $\text{LaBr}_3(\text{Ce})$
204 deposition is set to 1.173 MeV and the energy of $\text{CsI}(\text{TI})$ de-

205 position to 1.332 MeV, and the coincidence pulse is the sum
 206 of the two. The pulses from the experiment correspond to the
 207 same energy shown in Fig. 5b. The calculation results agree
 208 well with the experimental results except a certain amount of
 209 jitter in the experimental pulses.

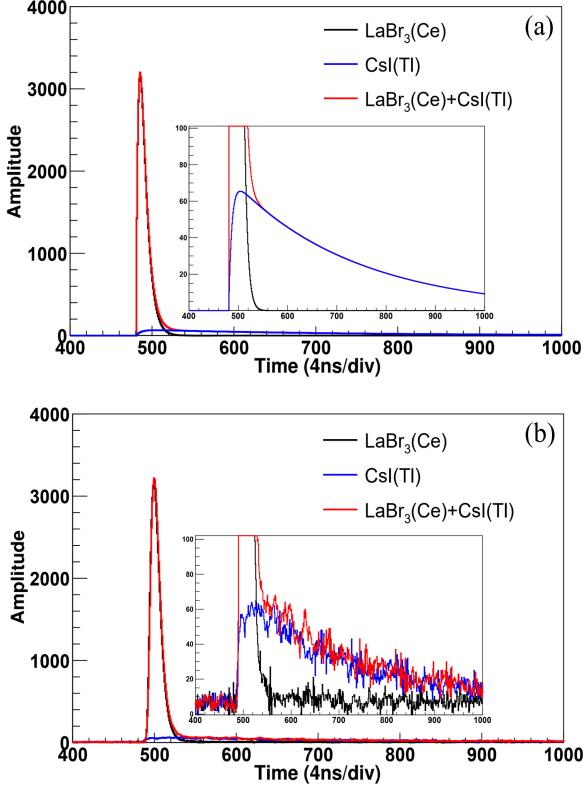


Fig. 5. (a) Three types of pulses of the phoswich detector predicted from Eq. 1. (b) Three types of pulses of the phoswich detector from the experiment. Black: $\text{LaBr}_3(\text{Ce})$ pulse; Blue: $\text{CsI}(\text{TI})$ pulse; Red: $\text{LaBr}_3(\text{Ce})+\text{CsI}(\text{TI})$ pulse. Inserted figure: expansion plot showing the pulse tail contributed from $\text{CsI}(\text{TI})$.

III. EXPERIMENTS AND RESULTS

211 The general-purpose digital data acquisition system
 212 (GDDAQ) developed by Peking University is used for data
 213 collection in our work [25–27]. This system consists of 16
 214 channels, each operating at a sampling rate of 2.5 million
 215 samples per second (250 MSPS), with incoming pulses dig-
 216 itized at 14-bit resolution. The properties of GDDAQ make
 217 it suitable for collecting $\text{LaBr}_3(\text{Ce})$ pulses. Using FPGA for
 218 pulse processing greatly simplifies equipment requirements
 219 and improves data acquisition efficiency [28].

220 The experimental diagram shown in Fig. 6 depicts the
 221 setup where the two ends of the detector are connected. One
 222 end is attached to a positive high voltage, while the other
 223 end is connected to a GDDAQ. Under the logic control of
 224 the FPGA (trigger/filter), the analog pulse is converted by the
 225 ADC into a digital pulse that is convenient for storage and
 226 analysis. The total time window for each pulse collection is

227 set to 10 μs , with a pulse trigger delay of 2 μs . This set en-
 228 sures that the time window is sufficiently long to capture the
 229 pulse from the $\text{CsI}(\text{TI})$ crystal ($\tau = 1000 \text{ ns}$) during each pulse
 230 acquisition. Considering the fluctuation of noise, the baseline
 231 is usually set at 10% of the maximum range, rather than at
 232 the zero position. We primarily store the acquired pulses to
 233 analyze flexibly in the later stage at each measurement.

A. ^{60}Co and ^{137}Cs Measurements

234 The phoswich detector was tested using radioactive sources
 235 including ^{60}Co ($1.92 \mu\text{Ci}$) and ^{137}Cs ($1.94 \mu\text{Ci}$) with the volt-
 236 age set to $+850 \text{ V}$. The radiation sources is positioned about
 237 30 cm from the detector's front surface, with count rates ap-
 238 proximately 600 counts per second (cps) for ^{60}Co and 650
 239 cps for ^{137}Cs .

1. Pulse Shape Discrimination

241 A total of 170K events were accumulated from the ^{137}Cs
 242 radioactive source to analyze and discriminate three types of
 243 pulses from the phoswich detector. The source was placed
 244 in front of the detector during the measurement. These
 245 three types of pulses obtained under the voltage condition are
 246 shown in Fig. 5b.

247 To achieve excellent anti-coincidence effects, the integra-
 248 tion interval widths for T_1 , T_2 , and T_3 are set at 120 ns, 240
 249 ns and 1200 ns in accordance with our calculations. The
 250 scatter plot of the FCR-SCR two-dimension plot for ^{137}Cs
 251 is clearly presented in Fig. 7. Region 1, 2 represent single
 252 events in $\text{LaBr}_3(\text{Ce})$, $\text{CsI}(\text{TI})$. Region 3 shows coinci-
 253 dence events of $\text{LaBr}_3(\text{Ce})$ and $\text{CsI}(\text{TI})$. The scattered data dis-
 254 tribution in other regions primarily consists of two or more
 255 pulses detected within the event window because of the ac-
 256 cidental coincidence. Events in region 3 closer to region 1
 257 have shapes more similar to those of $\text{LaBr}_3(\text{Ce})$ pulses. Con-
 258 versely, events farther from region 1 are similar to the shapes
 259 of $\text{CsI}(\text{TI})$ pulses. From Fig. 7, we end up realizing that anti-
 260 coincidence only requires selecting our desired $\text{LaBr}_3(\text{Ce})$ -
 261 only events from the total events.

2. Energy Spectra

263 Although the $\text{LaBr}_3(\text{Ce})$ crystal exhibits relatively high de-
 264 tection efficiency and reasonable energy resolution compared
 265 to other typical scintillation crystals, it has internal radiation
 266 due to the natural abundance of ^{138}La and ^{227}Ac decay prod-
 267 ucts, which contribute to the inevitable background events
 268 [29–31]. The background count rate is about 80 cps and its
 269 characteristic peaks will appear in the energy spectra.

271 The energy spectra are obtained using QDC. The integra-
 272 tion interval width is set to 120 ns, allowing for nearly full
 273 integration of the pulses captured by the $\text{LaBr}_3(\text{Ce})$ scin-
 274 tillator. Energy calibration is performed based on the channels of
 275 the $\text{LaBr}_3(\text{Ce})$. The results are shown in Fig. 8. Each figure

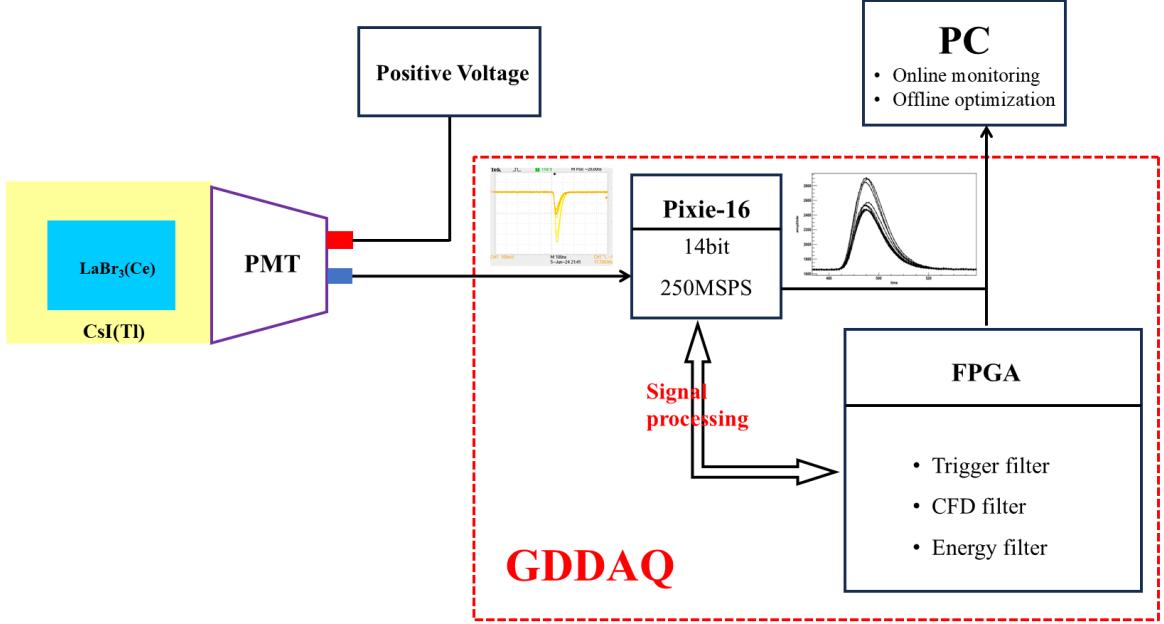


Fig. 6. Diagram of the digital data acquisition system.

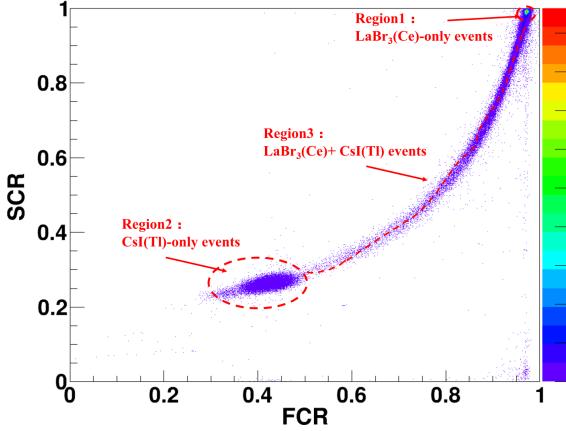


Fig. 7. Scatter plot of the FCR-SCR two-dimension plot for ^{137}Cs . Region 1 consists of $\text{LaBr}_3(\text{Ce})$ -only events, Region 2 consists of only $\text{CsI}(\text{Ti})$ -only events, and Region 3 consists of " $\text{LaBr}_3(\text{Ce})+\text{CsI}(\text{Ti})$ " events (coincidence).

276 contains four energy spectra, including the raw spectrum, the
 277 spectrum after Compton suppression, the $\text{CsI}(\text{Ti})$ -only spec-
 278 trum and the coincidence events spectrum. It can be seen
 279 that the $\text{CsI}(\text{Ti})$ events are concentrated at the low-energy end
 280 and form distinct peaks. Moreover, the characteristic peaks
 281 of 1436 keV γ and α emitter contaminants are still presented
 282 in both figures. By selecting the intervals where $\text{FCR} \geq 0.97$
 283 and $\text{SCR} \geq 0.96$ from Fig. 7, the spectrum after Compton
 284 suppression is obtained. The energy resolutions of this detec-
 285 tor are 3.7% (~ 662 keV), 3.1% (~ 1173 keV), 2.8% (~ 1332
 286 keV) before and after Compton suppression.

287 However, when the radioactive source is placed at 5 cm

288 away from the detector, the ^{60}Co energy spectrum after
 289 Compton suppression will be narrow at the photopeaks, while
 290 ^{137}Cs does not exhibit this feature shown in Fig. 8 inserted
 291 figures. The energy resolutions are 3.8% for 662 keV, 3.7%
 292 for 1173 keV and 3.2% for 1332 keV before Compton sup-
 293 pression in the distance of 5 cm. After Compton suppression,
 294 the energy resolutions are 3.8% for 662 keV, 3.1% for 1173
 295 keV and 2.8% for 1332 keV. These results indicate an energy
 296 resolution worsening between 17% and 11% at the ^{60}Co spec-
 297 trum. Only by increasing the distance can the phenomenon be
 298 eliminated, which will be discussed in Sect. IV A.

B. In-beam measurement

300 In order to benchmark the effect of cosmic anti-
 301 coincidence in the high-energy γ rays range of the phoswich
 302 detector, we also conducted an in-beam measurement. A fu-
 303 sion evaporation reaction experiment was conducted at the
 304 China Institute of Atomic Energy. The experiment measured
 305 the reaction $^{11}\text{B} + ^{142}\text{Ce}$ at $E_{beam} = 52$ MeV, with our de-
 306 tector placed at 60 degrees parallel to the beam line and a
 307 distance of 25 cm from the target within reasonable limits
 308 of space. The core goal of the measurement spectrum is
 309 mainly focused on the γ rays above 10 MeV, which corre-
 310 spond to GDR γ rays. The data acquisition system still used
 311 GDDAQ for collection, with the voltage adjusted to +600 V
 312 to ensure that high-energy pulses could be captured within
 313 the dynamic range. In the beam experiment measurement,
 314 the overall count rate fluctuated within the range of 3000 \sim
 315 4500 cps. Approximately 2.45×10^8 pulses were collected
 316 by measuring for 23 hours.

317 As shown in Fig. 9, the blue energy spectrum represents

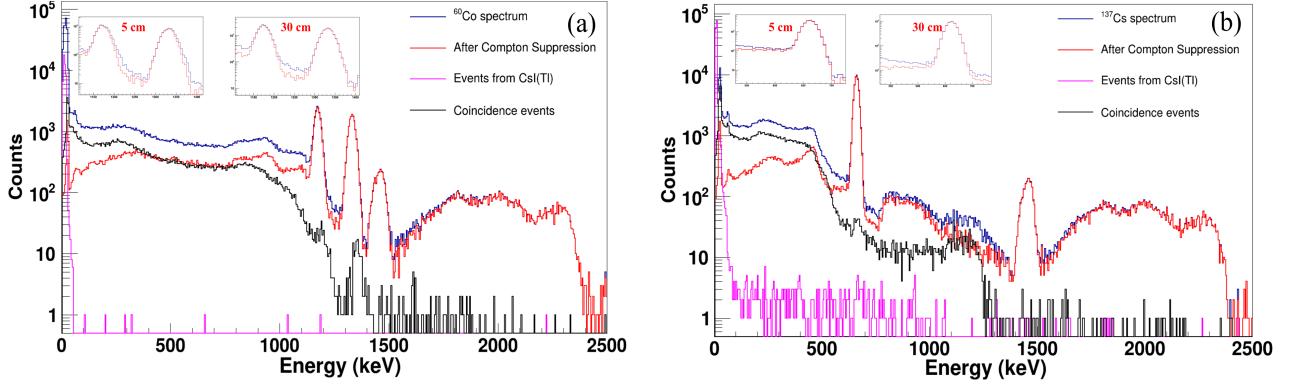


Fig. 8. The spectra from ^{60}Co and ^{137}Cs . The distance is 30 cm between the radioactive source and the surface of the detector. Inserted figure: The photopeak spectrum at different distances.

318 the in-beam spectrum, while the red spectrum corresponds to
 319 the blue one after anti-coincidence. Since the low collection
 320 efficiency in the high-energy region (>10 MeV), most of the
 321 pulse data is concentrated below 2 MeV, with a difference of
 322 5 to 6 orders of magnitude. Even with a broader bin width,
 323 some characteristic peaks can still be observed below 2 MeV,
 324 and they become even more distinct after anti-coincidence.
 325 We have also measured the background spectrum in our labo-
 326 ratory (black one) with the same time, and the magenta one is
 327 the γ -only background spectrum after anti-coincidence. Ad-
 328 ditionally, we used Geant4 to simulate the muon energy spec-
 329 trum and the decay of $^{138}\text{La}/^{227}\text{Ac}$ in the detector to confirm
 330 that the peak in the high-energy region originates from cos-
 331 mic rays, and the results were well confirmed (green one).
 332 The simulation above 20 MeV is higher than the experimen-
 333 tal results from the fact that we do not have an ideal setup for
 334 realistic environments.

335

IV. DISCUSSION

336

A. Energy resolution of cascade γ -rays

337 In Fig. 8, we measured the energy spectrum with the ra-
 338 dioactive source at different distances. We found that the en-
 339 ergy resolution of cascade γ rays degrades when the source
 340 is close to the detector but improves after Compton suppres-
 341 sion. The scatter plots of SCR-Energy two-dimension plot
 342 would help us analyze this phenomenon. As shown in Fig.
 343 10a and Fig. 10b, they provide both energy information on
 344 the x-axis and the distribution of different types of events on
 345 the y-axis from the experiment. Taking Fig. 10a as an ex-
 346 ample, we think the $\text{LaBr}_3(\text{Ce})$ -only events are distributed in
 347 $\text{SCR} > 0.96$, the $\text{CsI}(\text{Ti})$ -only as $\text{SCR} < 0.3$, and others are
 348 coincidence events. In addition, line-1 and line-2 represent
 349 the 1173 keV and 1332 keV γ rays continuously under-
 350 going multiple Compton scattering in the $\text{LaBr}_3(\text{Ce})$ crystal and
 351 captured by the $\text{CsI}(\text{Ti})$ crystal until they are all deposited in
 352 $\text{CsI}(\text{Ti})$. The reason why the two trends eventually merge in
 353 the $\text{CsI}(\text{Ti})$ -only events and cannot be distinguished is that the
 354 QDC selection range is not properly adapted for the $\text{CsI}(\text{Ti})$
 355 pulses. Line-3 is from the sum peak, so it is inferred that the
 356 total energy in the phoswich detector is 2505 keV in region
 357 1 (two dark dots). This indicates that both crystals simulta-
 358 neously captured the two cascade γ rays. The pulses in the
 359 previous Fig. 5b were also picked from these regions dis-
 360 cussed based on Fig. 10a. Fig. 10a also clearly demonstrates
 361 the energy deposition characteristics of γ rays entering the
 362 phoswich detector. Maybe they are all in $\text{LaBr}_3(\text{Ce})$, maybe
 363 they are all in $\text{CsI}(\text{Ti})$, or maybe they are more likely that
 364 Compton scattering occurs in one to be captured by the other
 365 completely or partly. Since the SCR interval for Compton
 366 suppression is selected to be above 0.96, it can be seen that
 367 the narrowing of the photopeak after suppression is caused by
 368 region 1 (Fig. 7). However, Fig. 10b shows a very clean dis-
 369 tribution compared with Fig. 10a because of the single γ ray
 370 of ^{137}Cs .

371 In order to better understand the reasons for optimizing en-
 372 ergy resolution after Compton suppression, the Geant4 simu-

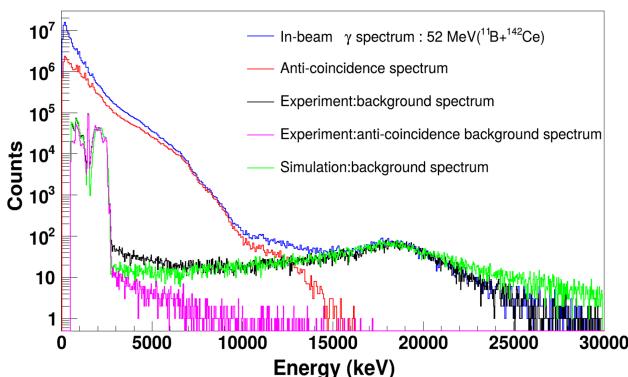


Fig. 9. Energy spectra from in-beam, background and Geant4 simulation. Blue: The raw spectrum from in-beam experimental mea-
 surements. Red: The in-beam spectrum after anti-coincidence. Black: The background spectrum from experiment. Magenta: The background spectrum after anti-coincidence. Green: The background spectrum from Geant4 simulation.

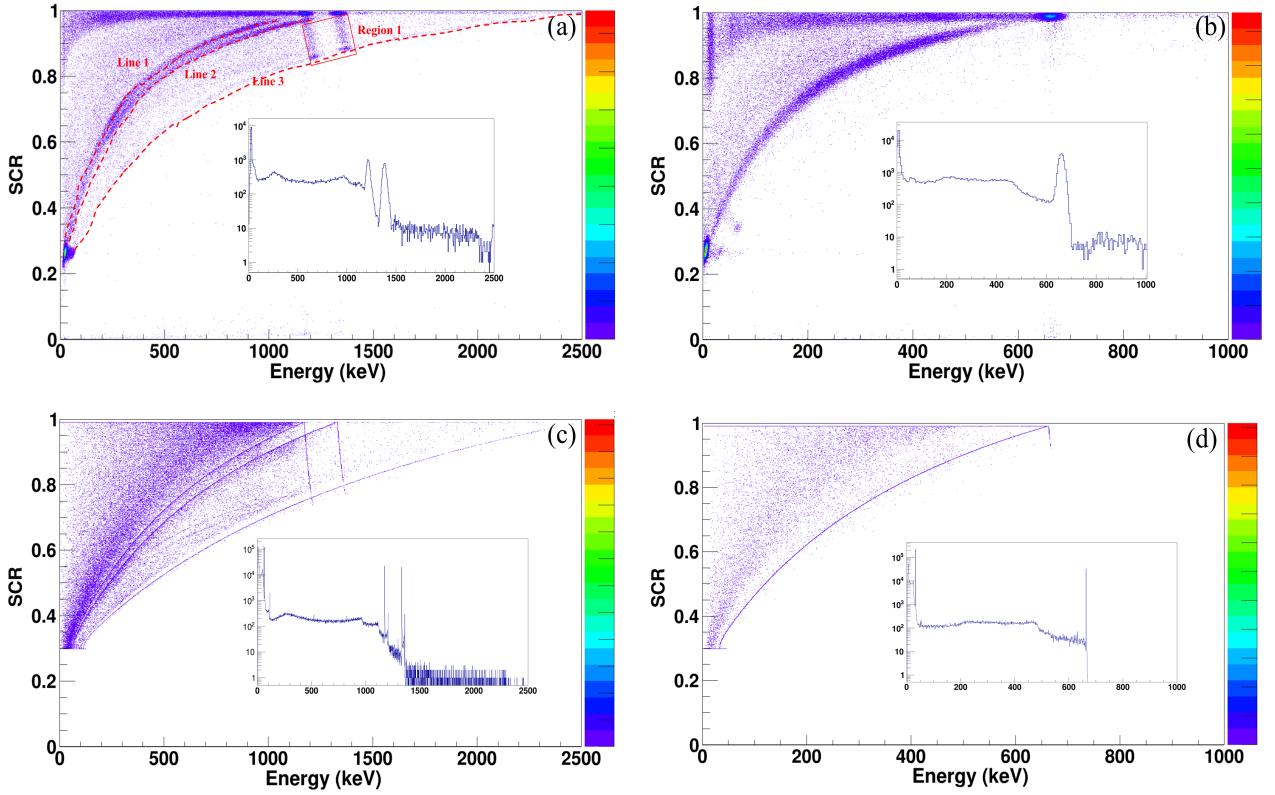


Fig. 10. Scatter plots of SCR-Energy two-dimension plot from experiments (top panel) and simulations (bottom panel) for ^{60}Co (a and c) and ^{137}Cs (b and d). The radiation source is 5 cm away from the surface of the detector. Inserted figure: energy projection spectrum.

373 lation is used to help analyze the experimental data because
 374 it can output physical information [32, 33]. We obtained the
 375 energy deposition results through simulation and converted
 376 them to a pulse using Eq. 1, for which the pulses are con-
 377 sistent with the experimental results (Fig. 5). The simulated
 378 PSA scatter plots are shown in Fig. 10c and Fig. 10d. Similar
 379 to region 1 in Fig. 10a, this phenomenon suggests that the
 380 $\text{LaBr}_3(\text{Ce})$ crystal captures one γ , while the $\text{CsI}(\text{TI})$ crystal
 381 captures the other. Specifically, when this phoswich detec-
 382 tor was exposed to the ^{60}Co radiation source with a strong
 383 cascading effect, the coincident events at 1173 keV and 1332
 384 keV between the two scintillators were clearly observed. For
 385 example, the 1173 keV γ ray was captured by the $\text{LaBr}_3(\text{Ce})$
 386 scintillator, while the 1332 keV cascade γ ray was captured
 387 by the $\text{CsI}(\text{TI})$ scintillator. So, they will eventually converge
 388 on line-3. The energy projection spectrum for ^{60}Co simula-
 389 tion without energy broadening in Fig. 10c inserted figure
 390 shows one peak appear after each photopeak. After broad-
 391 ening, such events are swamped by the tail of the photopeak,
 392 which worsens the resolution; therefore, the energy resolution
 393 will be optimized after excluding the influence of cascade γ
 394 rays (Sec. III A 2). However, the QDC integration width is
 395 the primary cause of this phenomenon. A wider integration
 396 width can partially mitigate the effect of $\text{CsI}(\text{TI})$ events on
 397 the $\text{LaBr}_3(\text{Ce})$ photopeak's energy resolution, but the ability
 398 to distinguish between the two pulses deteriorates. In conclu-
 399 sion, the phoswich detector's energy resolution for cascade γ

400 rays decreases when the radiation source is close. The energy
 401 resolution will become better when the radioactive source is
 402 pulled away from the distance because the probability of cap-
 403 turing these two γ rays decreases.

B. Compton suppression

404 We present the energy spectra measured using the ^{60}Co
 405 source and the ^{137}Cs source, and extract the spectra of dif-
 406 ferent events using the FCR-SCR method in Fig. 8. After
 407 Compton suppression, the events in the Compton continuum
 408 are significantly reduced. For Compton continuum, we de-
 409 fined the energy range as 170 ~ 490 keV for 662 keV; 210
 410 ~ 963 keV for 1173 keV; and 214 ~ 1118 keV for 1332 keV
 411 from the back-scattering peak to the Compton edge [34]. The
 412 Compton suppression factor can be defined as the following:

$$413 \quad \zeta = \frac{I_{us}}{I_s} \times 100\% \quad (4)$$

414 where ζ is the suppression factor. I_{us} is the number of
 415 counts in energy E of the unsuppressed spectrum and I_s is
 416 the number of counts in energy E of the suppressed spectrum.
 417 The higher the value of ζ , the more ideal the suppression ef-
 418 fect. As shown in Fig. 11, in order to highlight the count

420 variation at the photopeak position, the energy interval selection range is appropriately extended from the Compton continuum to the photopeak. In the Compton continuum, 50 bins are selected as one point, and the error bar for each point is obtained using the error propagation formula.

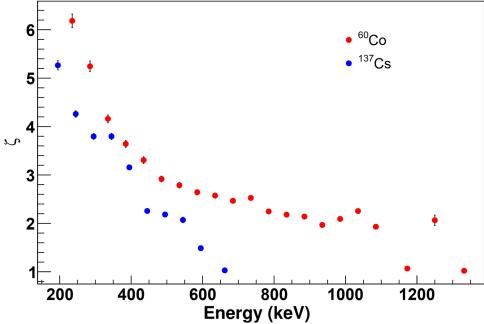


Fig. 11. The Compton suppression factor of the phoswich detector for ^{60}Co (red dots) and ^{137}Cs (blue dots).

425 From Fig. 11, it can be seen that the value of ζ is close to 426 1 at the photopeaks position, indicating that there is almost 427 no loss at the photopeaks (the suppression factors are 1.04 428 for 662 keV; 1.06 for 1173 keV; 1.02 for 1332 keV). There 429 is a certain suppression effect between the two photopeaks of 430 ^{60}Co , likely due to scattering from the 1436 keV photopeak 431 (Fig. 10). The suppression factor has significantly increased 432 in the Compton continuum due to the effective suppression. 433 For the photopeak of ^{137}Cs , the suppression in this energy re- 434 gion ranges from 2~5 times. For the two photopeaks of ^{60}Co , 435 the suppression effect of the Compton continuum reaches 436 2~6 times. Due to the detector's structural design, a 1.0 cm 437 thick CsI(Tl) top layer is added near the radiation source to 438 capture back-scattering events. Therefore, as can also be seen 439 from the Fig. 11, a certain degree of suppression effect is 440 also achieved in the Compton edge (corresponding to back- 441 scattering events). The suppression effect of the low-energy 442 part in the Compton continuum is more effective than that of 443 the high-energy part. This indicates that small-angle scatter- 444 ing events have a higher detection efficiency compared with 445 back-scattering events.

446

C. Cosmic rays anti-coincidence

447 As shown in Fig. 9, the γ rays with energy more than 10 448 MeV are completely buried by cosmic rays and cannot be ob- 449 served in the in-beam spectrum. As we all know, atmospheric 450 cosmic ray muons constantly pass through the detector, caus- 451 ing energy loss within it, and the incident muons follow a 452 zenith angle distribution from top to bottom [35, 36]. For the 453 phoswich detector, muons entering from top to bottom will 454 generate two types of pulses: 1) Only CsI(Tl) crystal cap- 455 ture; 2) Captured by both CsI(Tl) and LaBr₃(Ce) crystals. 456 As shown in Fig. 12, in terms of the pulse amplitude and 457 width, the muon pulse shows a clear distinction from the γ 458 pulse. Therefore, by using the FCR-SCR method to select

459 the LaBr₃(Ce)-only events, we can effectively filter out the 460 components from cosmic rays in the energy spectrum.

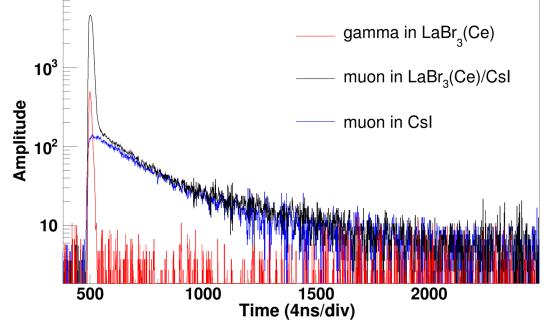


Fig. 12. Pulse comparison of muon with γ measured in the phoswich detector in the phoswich detector. Red: γ rays interacting only with the LaBr₃(Ce) crystal; Black: muon interacting with both crystals; Blue: muon interacting only with the CsI(Tl) crystal.

461 The resulting energy spectrum is shown as the red spectrum 462 in Fig. 9 after selecting the LaBr₃(Ce)-only events. For en- 463 ergy greater than 10 MeV in the background spectrum, there 464 are about 14,600 events before anti-coincidence, while only 465 60 events remained after anti-coincidence. This means that 466 almost all cosmic rays can be rejected. Therefore, the sup- 467 pression effect will also be reflected in the in-beam spectrum 468 because of the same measured time in the high-energy region. 469 Due to the effective anti-coincidence effect of the background 470 spectrum, the in-beam spectrum presents a 'bump' above 10 471 MeV which is characteristic of GDR γ after anti-coincidence 472 [37]. This fully demonstrates that, under the characteristics 473 of the structure, cosmic rays can be eliminated by means of 474 PSA and it can be used to study high-energy γ such as GDR 475 γ rays spectrum. In experiments, the CASCADE program, 476 based on statistical model theory, is commonly used to fit the 477 observed high-energy γ spectra and extract the GDR parame- 478 ters (resonance energy E; shape width Γ ; strength S) [37, 38]. 479 This could be a point for future research, but it is essential to 480 ensure a sufficient amount of measurement data.

481

V. SUMMARY

482 We introduced a novel anti-coincidence shielding 483 phoswich detector which consists of the LaBr₃(Ce) and 484 CsI(Tl) scintillator. The LaBr₃(Ce) scintillator is selected as 485 the main crystal and the CsI(Tl) scintillator as the shielding 486 crystal, so it can realize excellent discrimination of pulses to 487 achieve the anti-coincidence. In the experiment, pulses were 488 collected using the GDDAQ, energy spectra were obtained 489 via the QDC, and pulse discrimination was performed using 490 the FCR-SCR method. Since the integration width of the se- 491 lected region is determined by the LaBr₃(Ce) pulse width in 492 QDC calculations, CsI(Tl) events are primarily concentrated 493 in the low energy region of the spectrum in the radioative 494 source measurement. The energy resolution of the detector 495 is 3.7% for 662 keV of ^{137}Cs , while achieving 3.1% for 496 1173 keV and 2.8% for 1332 keV of ^{60}Co after excluding

497 the influence of cascade γ rays. The detector suppresses the
 498 Compton continua of $^{60}\text{Co}/^{137}\text{Cs}$ by a factor of 2~5 times
 499 with almost no loss of the photopeaks. Furthermore, we
 500 conducted an experiment focusing on the high-energy γ rays
 501 (> 10 MeV) emitted in the fusion evaporation reaction ^{11}B
 502 + ^{142}Ce at $E_{beam} = 52$ MeV in order to study the shielding
 503 effect of cosmic rays. We successfully applied the PSD to
 504 mitigate the impact of high-energy cosmic rays and almost
 505 all cosmic rays can be rejected by filtering events above
 506 10 MeV. After the anti-coincidence process, the energy
 507 spectrum clearly displayed the 'bump' feature of the GDR γ
 508 rays.

509 This phoswich detector not only can suppress the Com-
 510 ton continuum, which is crucial for enhancing measurement
 511 sensitivity in some low level radioactivity measurements, but
 512 also realizes anti-coincidence shielding of cosmic rays in the
 513 high-energy range, such as the measurement of high-energy
 514 γ rays such as GDR γ rays.

515 [1] S.Bender, B.Heidrich, Ünlü K., Compton suppressed LaBr_3 565
 516 detection system for use in nondestructive spent fuel assay. 566
 517 *Nucl. Instrum. Methods Phys. Res. A.* **784**, 474-481 (2015). 567
 518 [doi: *https://doi.org/10.1016/j.nima.2014.12.025*](https://doi.org/10.1016/j.nima.2014.12.025) 568

519 [2] J. Parus, J. Kierzek, W. Raab, *et al.*, A dual purpose Compton 569
 520 suppression spectrometer. *J. Radioanal. Nucl. Chem.* **258**, 123- 570
 521 132(2003).<https://doi.org/10.1023/a:1026270428392> 571

522 [3] Y. Li, W.D. Huang, S.H. Shi, *et al.*, The level structure of ^{76}Se 572
 523 from ^{76}Br γ -decay. *Nucl. Sci. Tech.* **9**, 199-208(1998). 573

524 [4] De Voigt M J A, Bacelar J C, Micek S L, *et al.*, 574
 525 A novel compact Ge-BGO Compton-suppression spectrom- 575
 526 eter. *Nucl. Instrum. Methods Phys. Res. A.* **356**, 362- 576
 527 375(1995).[https://doi.org/10.1016/0168-9002\(94\)01204-0](https://doi.org/10.1016/0168-9002(94)01204-0) 577

528 [5] Tabor S L, BGO suppressed gamma detector ar- 578
 529 rays. *Nucl. Instrum. Methods Phys. Res. B.* **24**, 1031- 579
 530 1034(1987).[https://doi.org/10.1016/S0168-583X\(87\)80305-1](https://doi.org/10.1016/S0168-583X(87)80305-1) 580

531 [6] Zhu L, Huang Z, Hou L, *et al.*, Study of Giant Dipole Reso- 581
 532 nance in Hot Rotating Nucleus ^{132}Ce . *Chin. Phys. Lett.* **12**, 148- 582
 533 151(1995).[10.1088/0256-307X/12/3/006](https://doi.org/10.1088/0256-307X/12/3/006) 583

534 [7] Spicer, B.M., The Giant Dipole Resonance. *Adv. Nucl. 584
 535 Phys.*(1969).https://doi.org/10.1007/978-1-4684-8343-7_1 585

536 [8] Krasznahorkay A J, Krasznahorkay A, Csatlós M, *et al.*, An 586
 537 Update of the Hypothetical X17 Particle.Universe. **10**, 409- 587
 538 (2024).<https://doi.org/10.3390/universe10110409> 588

539 [9] Mason, W.M., Kernel, G., Black, J.L., *et al.*, The giant dipole 589
 540 resonance and isospin in $^{89}\gamma(p, \gamma)^{90}\text{Zr}$. *Nucl. Phys.A.* **135**, 590
 541 (1969).[https://doi.org/10.1016/0375-9474\(69\)90158-4](https://doi.org/10.1016/0375-9474(69)90158-4) 591

542 [10] B. L. Berman and S. C. Fultz, Measurements of the giant dipole 592
 543 resonance with monoenergetic photons. *Rev. Mod. Phys.* **47**, 593
 544 713(1975).<https://doi.org/10.1103/RevModPhys.47.713> 594

545 [11] Warburton W K, Grudberg P M., Current trends in devel- 595
 546 oping digital pulse processing electronics for semiconduc- 596
 547 tor detectors. *Nucl. Instrum. Methods Phys. Res. A.* **568**, 350- 597
 548 358(2006).<https://doi.org/10.1016/j.nima.2006.07.021> 598

549 [12] Koskelo M J, Koskelo I J, Sielaff B., Comparison 599
 550 of analog and digital pulse processing systems using 600
 551 pulsers. *Nucl. Instrum. Methods Phys. Res. A.* **422**, 373- 601
 552 378(1999).[https://doi.org/10.1016/S0168-9002\(98\)00986-3](https://doi.org/10.1016/S0168-9002(98)00986-3) 602

553 [13] J.Glodo, W.W.Moses, Effects of Ce Concentration on Scintil- 603
 554 lation Properties of $\text{LaBr}_3:\text{Ce}$. *IEEE Trans. Nucl. Sci.* **52**, 1805- 604
 555 1808(2005).[10.1109/NSSMIC.2004.1462374](https://doi.org/10.1109/NSSMIC.2004.1462374) 605

556 [14] Min, Sujung, Bumkyung Seo, Changhyun Roh, *et al.*, 606
 557 phoswich Detectors in Sensing Applications. *Sensors.* **21**, 607
 558 4047(2021).<https://doi.org/10.3390/s21124047> 608

559 [15] H.D.Wang, Jing-Bin Lu, R.P. Li, *et al.*, A phoswich 609
 560 design using real-time rise time discrimination 610
 561 for Compton suppression of $\text{LaBr}_3:\text{Ce}$ detec- 611
 562 tor. *Nucl.Instrum. Methods Phys.Res.A.* **1048**:167920(2023). 612
 563 <https://doi.org/10.1016/j.nima.2022.167920> 613

564 [16] H.D.Wang, Jing-Bin Lu, R.P.Li, *et al.*, An entrance win- 614
 565 dow surrounded phoswich design for efficient large-angle
 566 Compton-suppressed and low-background GAGG: Ce detec-
 567 tor. *Nucl. Instrum. Methods Phys.Res.A.* **1055**:168542(2023).
 568 <https://doi.org/10.1016/j.nima.2023.168542>

569 [17] Farsoni, A.T., Alemayehu, B., Alhawsawi, A. *et al.*, A 570
 571 compton-suppressed phoswich detector for gamma spec- 572
 572 troscopy. *J. Radioanal. Nucl. Chem.*, **296**, 63-68 (2013).
 573 <https://doi.org/10.1007/s10967-012-2009-2>

574 [18] Jia Xu, Jun Liu, Xiulian Chen, A well typed phoswich detector 575
 575 consisting of CsI and plastic scintillators for low level radioac- 576
 576 tivity measurements. *Appl. Radiat. Isot.* **169**, 109462(2021).
 577 <https://doi.org/10.1016/j.apradiso.2020.109462>

578 [19] Paul Lecoq, Development of new scintillators for medical 579
 579 applications. *Nucl. Instrum. Methods Phys.Res.A.* **809**, 130- 580
 580 139(2016).<https://doi.org/10.1016/j.nima.2015.08.041>

581 [20] LI Tianxiao, Wu Hongyi, Zheng Yun, *et al.*, Study 582
 582 on Compton-suppressed phoswich Gamma-ray Detector of 583
 583 $\text{LaBr}_3(\text{Ce})\text{-CsI}(\text{Tl})$. *Nucl. Phys. Rev.* **40**, 73-77(2023). [10.11804/NuclPhysRev.40.20222021](https://doi.org/10.11804/NuclPhysRev.40.20222021)

584 [21] Davission C M, Gamma-Ray Absorption Coefficients. *Mod. 585
 585 Phys.* **24**, 79(1952).<https://doi.org/10.1103/RevModPhys.24.79>

586 [22] W. H. Miller, M. Diaz de Leon, Utilization of 587
 587 phoswich detectors for simultaneous, multiple radi- 588
 588 ation detection. *J. Radioanal. Nucl. Chem.* **264**, 163- 589
 589 167(2005).<https://doi.org/10.1007/s10967-005-0689-6>

590 [23] Leo W R, *Techniques for nuclear and particle physics experiments: a how-to approach*. (Springer Science & Business Media, 1994), pp.189-190

591 [24] M. Yoneyama, J. Kataoka, M. Arimoto, *et al.*, Evaluation 592
 592 of GAGG:Ce scintillators for future space applications. *J. Instrum.* **13**, (2018).[10.1088/1748-0221/13/02/P02023](https://doi.org/10.1088/1748-0221/13/02/P02023)

593 [25] H.Y. Wu, Z.H. Li, H. Tan, *et al.*, A general-purpose dig- 594
 594 ital data acquisition system (GDDAQ) at Peking Univer- 595
 595 sity. *Nucl.Instrum. Methods Phys.Res.A.* **975**, 164200(2020).
 596 <https://doi.org/10.1016/j.nima.2020.164200>

597 [26] H.Y. Wu, Z.H. Li, H. Tan, *et al.*, A general-purpose 598
 598 data acquisition system and a pulse analysis algorithm 599
 599 based on digitization (in Chinese). *Chin.Sci.Bull.* **66**, 3553- 600
 600 3560(2021).[10.1360/TB-2021-0552](https://doi.org/10.1360/TB-2021-0552)

601 [27] Di-Wen Luo, Hong-Yi Wu, Zhi-Huan Li, *et al.*, Perfor- 602
 602 mance of digital data acquisition system in gamma-ray spec- 603
 603 troscopy. *Nucl. Sci. Tech.* **32**, 79(2021).[10.1007/s41365-021-00917-8](https://doi.org/10.1007/s41365-021-00917-8)

604 [28] A. Al-Adili, F.-J. Hambach, S. Oberstedt, *et al.*, Compar- 605
 605 ison of digital and analogue data acquisition systems for 606
 606 nuclear spectroscopy. *Nucl.Instrum. Methods Phys.Res.A.* **624**, 684-690(2010).<https://doi.org/10.1016/j.nima.2010.09.126>

607 [29] Hao Cheng, Bao-Hua Sun, Li-Hua Zhu, *et al.*, Intrinsic 608
 608 background radiation of $\text{LaBr}_3(\text{Ce})$ detector via coinci- 609
 609 dence measurements and simulations. *Nucl. Sci. Tech.* **31**, 99- 610
 610

615 (2020).<https://doi.org/10.1007/s41365-020-00812-8>

616 [30] B.D. Milbrath, R.C. Runkle, T.W. Hossbach, *et al.*, 635
617 Characterization of alpha contamination in lanthanum 636
618 trichloride scintillators using coincidence measure- 637
619 ments.Nucl.Instrum. Methods Phys.Res.A.**547**, 504- 638
620 510(2005). <https://doi.org/10.1016/j.nima.2004.11.054>

621 [31] Y. -Y. Ji, H. -Y. Choi, Wanno Lee, *et al.*, Application 639
622 of a LaBr₃(Ce) Scintillation Detector to an Environmen- 640
623 tal Radiation Monitor.IEEE Trans. Nucl. Sci. **65**, 2021- 641
624 2028(2018).[10.1109/TNS.2018.2823322](https://doi.org/10.1109/TNS.2018.2823322)

625 [32] Allison, J, Amako, K, J. Apostolakis, *et al.*, Recent 642
626 developments in Geant4. Nucl.Instrum. Methods Phys.Res.A. **835**, 643
627 186-225(2016). <https://doi.org/10.1016/j.nima.2016.06.125>

628 [33] Allison J, Amako K, Apostolakis J E A, *et al.*, Geant4 de- 644
629 velopments and applications. IEEE Trans. Nucl. Sci. **53**, 270- 645
630 278(2006). [10.1109/TNS.2006.869826](https://doi.org/10.1109/TNS.2006.869826)

631 [34] Qiao C K, Wei J W, Chen L, An overview of the 646
632 compton scattering calculation. Cryst. **11**, 525(2021). 647
633 <https://doi.org/10.3390/cryst11050525>

634 [35] Prashant Shukla and Sundaresh Sankrith, Energy 635
636 and angular distributions of atmospheric muons at 637
638 the Earth.Int. J. Mod. Phys. A.**33**, 1850175(2018).
<https://doi.org/10.1142/S0217751X18501750>

638 [36] Bryan Olmos Yáñez and Alexis A. Aguilar-Arevalo, A method 639
639 to measure the integral vertical intensity and angular distribu- 640
640 tion of atmospheric muons with a stationary plastic scintilla- 641
641 tor bar detector. Nucl. Instrum. Methods Phys. Res. A. **987**, 642
642 164870(2021).<https://doi.org/10.1016/j.nima.2020.164870>

643 [37] Xia Haihong, Zhu Lihua, Huang Zheng-de, *et al.*, 644
644 Study of Giant Dipole Resonance in Hot Rotating Nu- 645
645 clei.Nucl.Phys.Rev.**15**, 266-273(1998).DOI: [10.11804/NuclPhysRev.15.04.266](https://doi.org/10.11804/NuclPhysRev.15.04.266)

647 [38] Bai J H, Niu Z M, Sun B Y, *et al.*, The de- 648
648 scription of giant dipole resonance key parameters 649
649 with multitask neural networks. Phys. Lett. B. **815**, 650
136147(2021).<https://doi.org/10.1016/j.physletb.2021.136147>